



SHORT NOTES

C H A P T E R

Refraction - Plane Surface

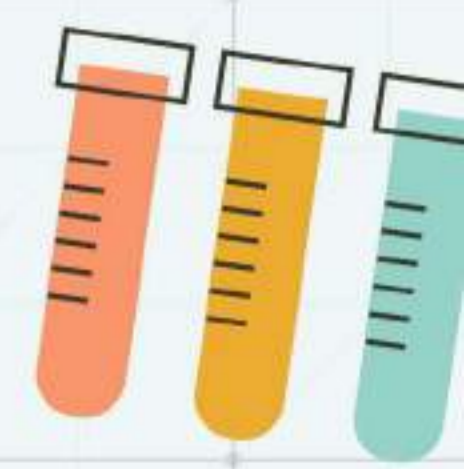
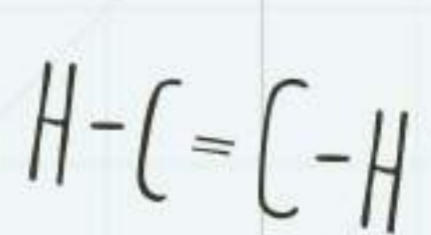
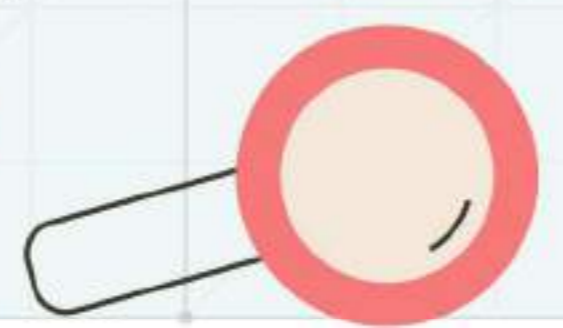
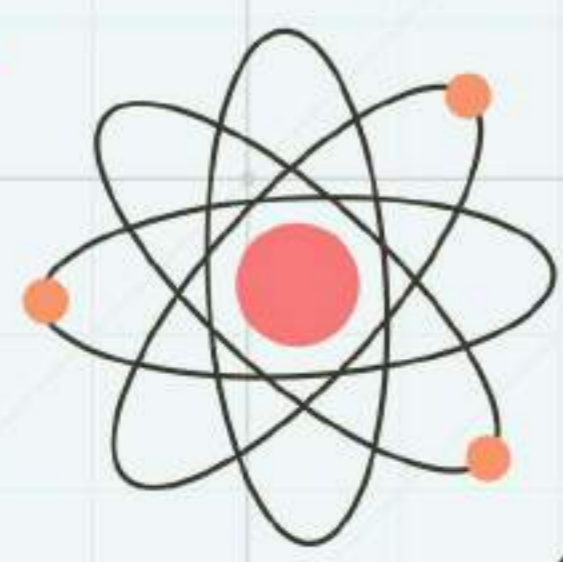
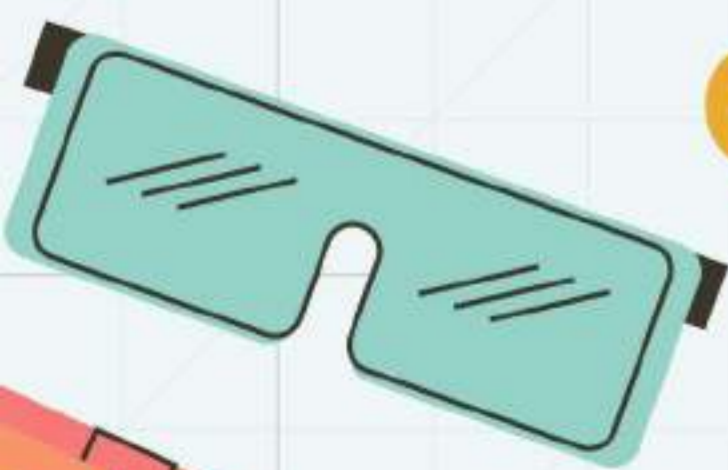
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when ray of light travels from one medium to other with or without bending

Refraction: Plane Surface \rightarrow focal length $= \infty$

Refractive index of a medium

$$\eta = \frac{\text{Speed of light in vacuum}}{\text{Speed of light in medium}} = \frac{c}{v}$$

medium 1 $\rightarrow \eta_1 = \frac{c}{v_1}$
 medium 2 $\rightarrow \eta_2 = \frac{c}{v_2}$

$\Rightarrow \eta_{12}$ = refractive index of medium 1 with respect to medium 2

$$\eta_{12} = \frac{\eta_1}{\eta_2} = \frac{c/v_1}{c/v_2} = \frac{v_2}{v_1}$$

$$\eta_{21} = \frac{v_1}{v_2}$$

- * Going from one medium to other medium
 - Speed of light \rightarrow change
 - wavelength \rightarrow change
 - frequency \rightarrow NOT CHANGE

So, $n_1 = \frac{c}{v_1} = \frac{c}{f \lambda_1} = \frac{f \lambda_0}{f \lambda_1}$

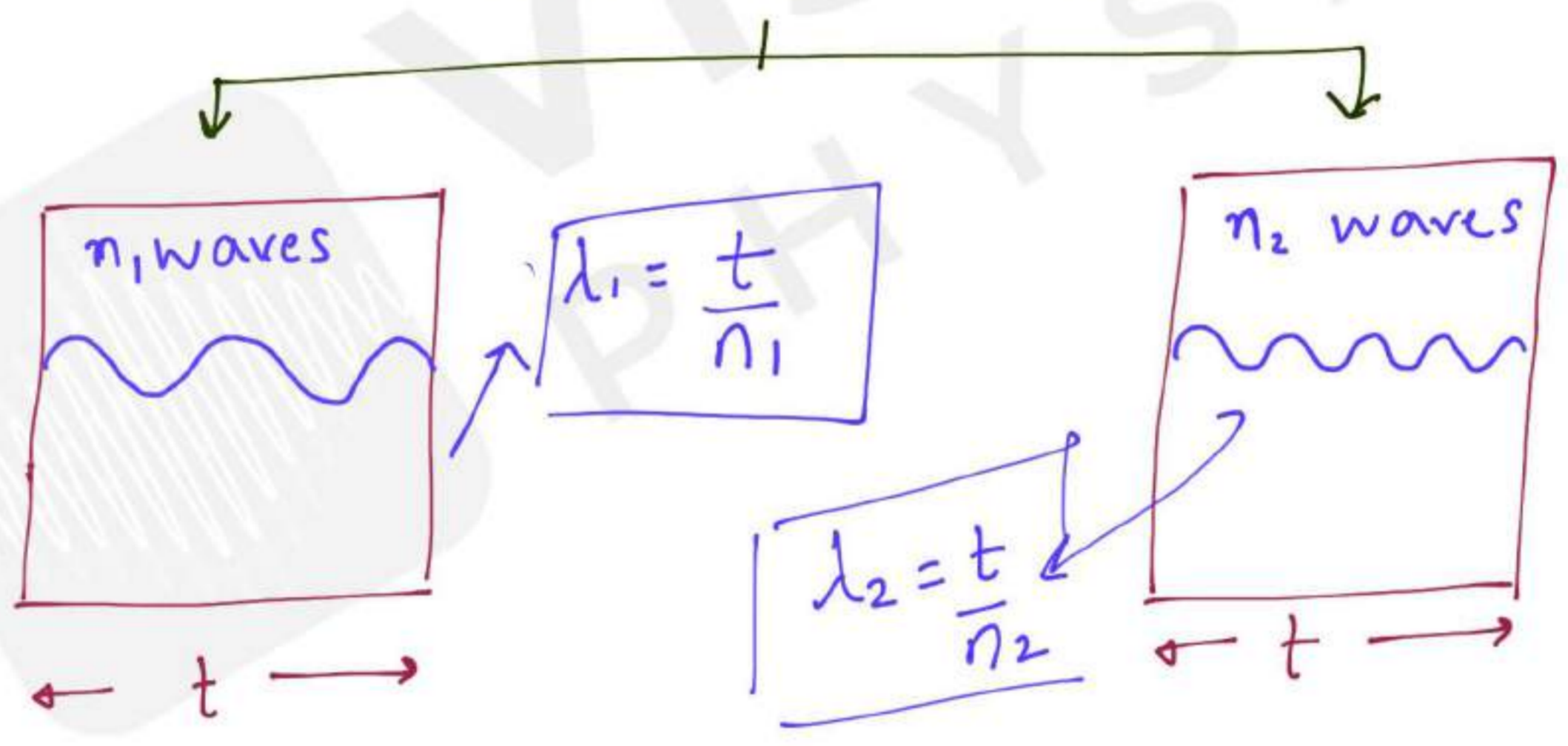
Annotations:

- f : frequency
- λ_1 : wavelength in medium 1
- λ_0 : wavelength in vacuum

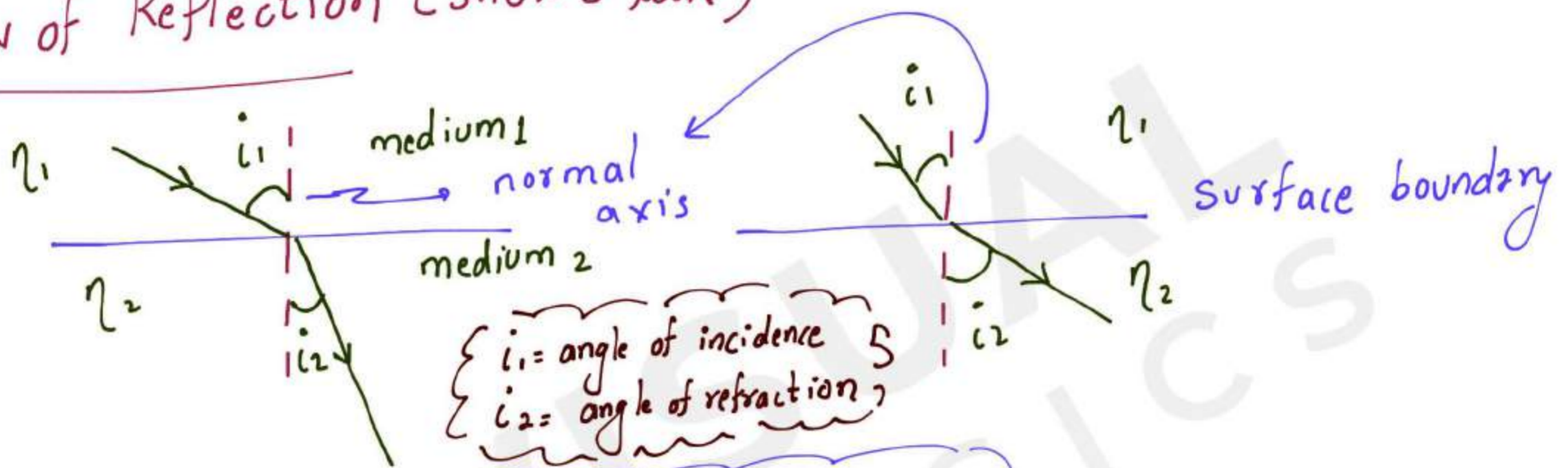
$\Rightarrow n_1 = \frac{\lambda_0}{\lambda_1}$

$\Rightarrow n_{12} = \frac{v_2}{v_1} = \frac{\lambda_2}{\lambda_1}$ *

waves in different slabs:



Law of Reflection (Snell's law)



Snell's law $\rightarrow \eta \sin i = \text{constant}$

or $\eta_1 \sin i_1 = \eta_2 \sin i_2$

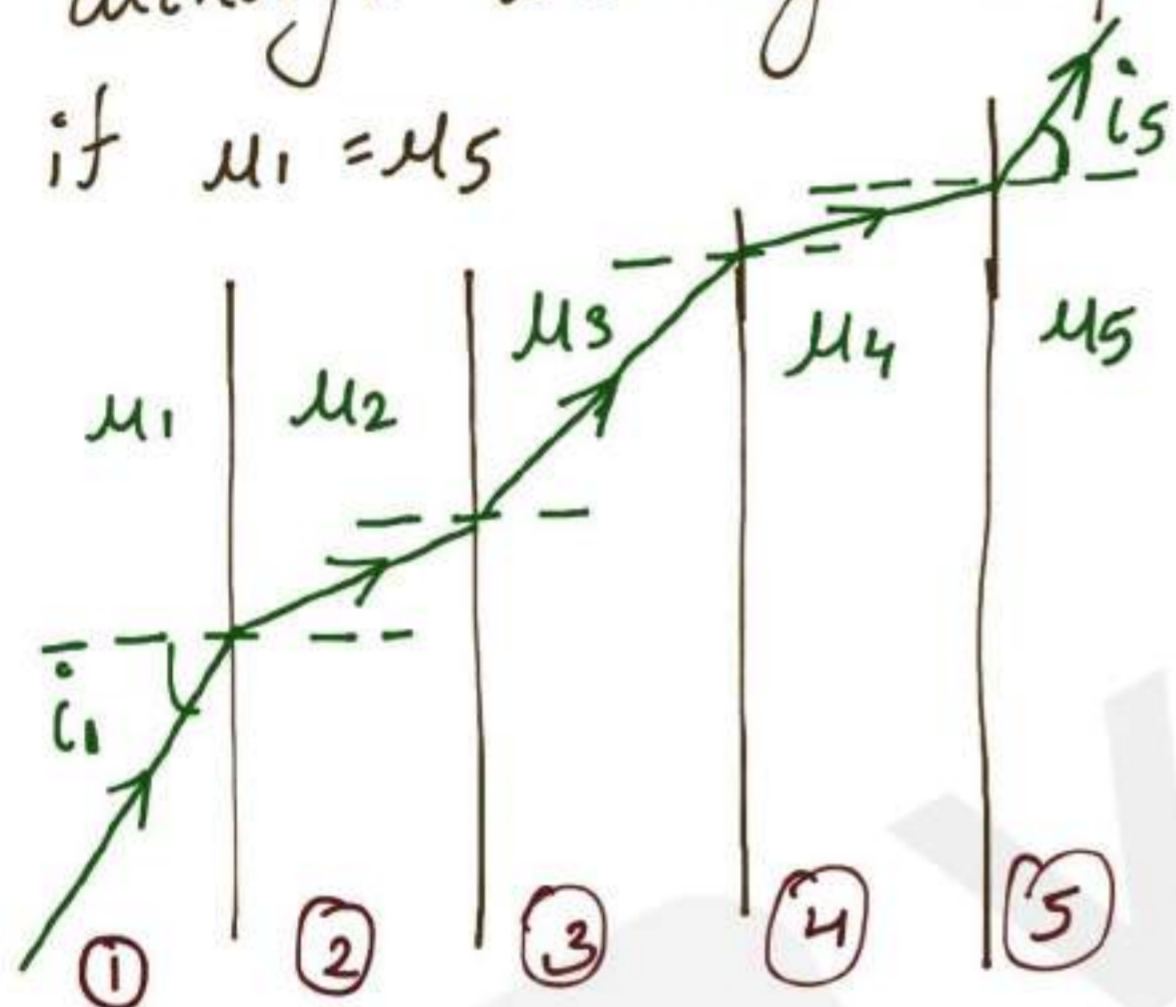
$$\frac{\sin i_1}{\sin i_2} = \frac{\eta_2}{\eta_1}$$

$\eta_1 > \eta_2$
 $\rightarrow i_2 > i_1$

$\eta_2 > \eta_1$
 $i_1 > i_2$

* $\eta_1 > \eta_2$
 ↓
 Denser medium
 ↳ rarer medium
 * vice-versa

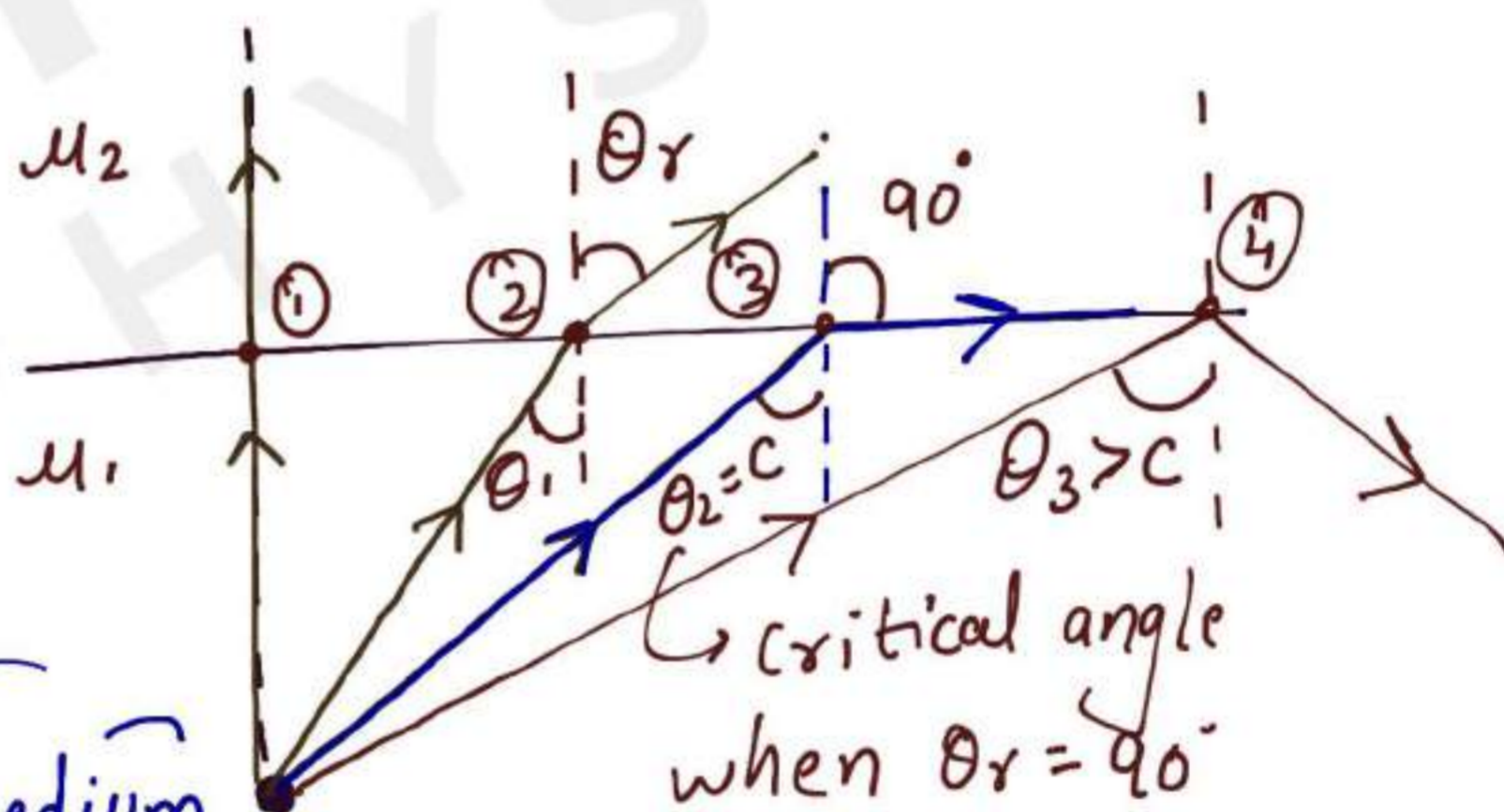
★ If the boundaries of the media are parallel, the emergent ray although laterally displaced is parallel to the incident ray if $\mu_1 = \mu_5$



$$\mu_1 \sin i_1 = \mu_5 \sin i_5$$

Critical angle & TIR:

$$\mu_2 < \mu_1$$



$$\frac{\sin C}{\sin 90^\circ} = \frac{\mu_2}{\mu_1}$$

$$\left\{ \begin{array}{l} \sin C = \frac{\mu_2}{\mu_1} = \frac{\text{RI of rarer medium}}{\text{RI of denser medium}} \end{array} \right.$$

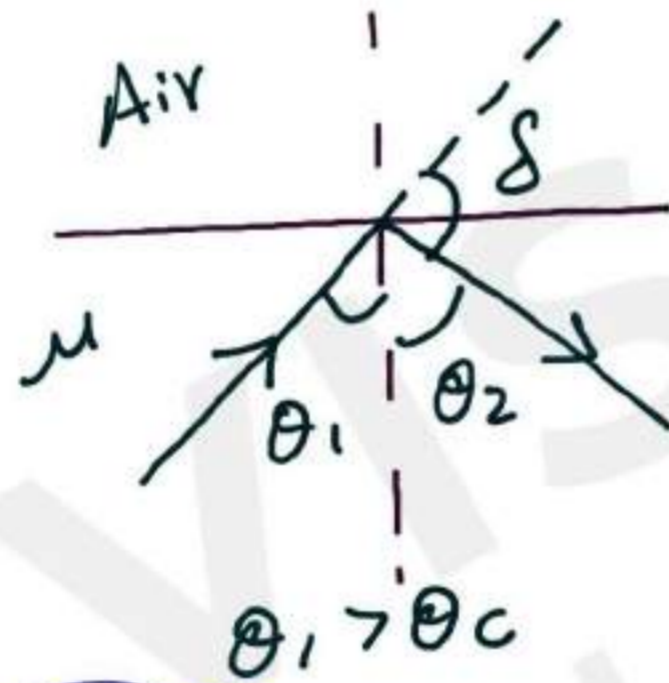
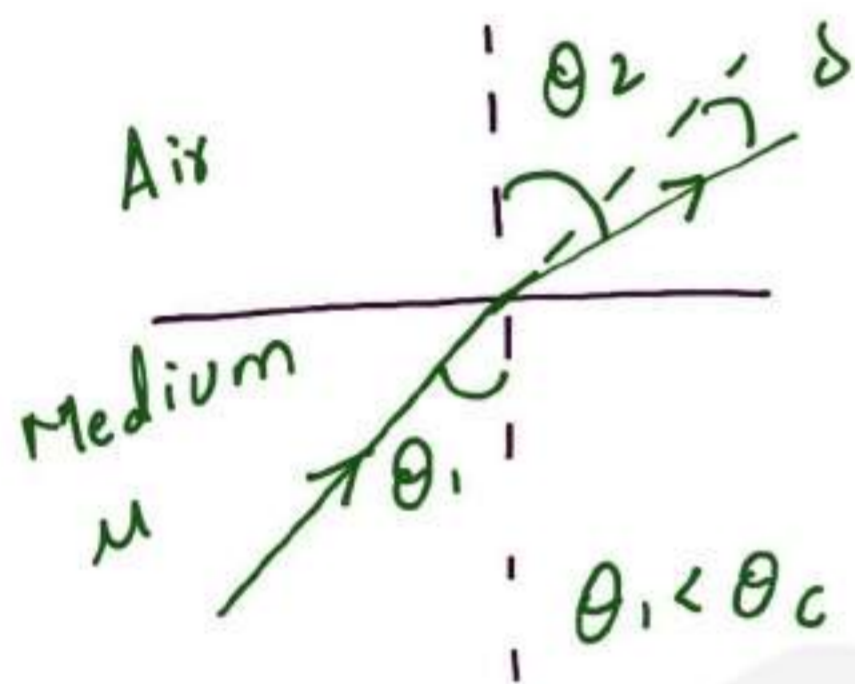
Deviation of ray due to Refraction

$$\delta = \theta_2 - \theta_1$$

$$\sin \theta_2 = \mu \sin \theta_1$$

$$\theta_2 = \sin^{-1}(\mu \sin \theta_1)$$

$$\delta = \sin^{-1}(\mu \sin \theta_1) - \theta_1$$

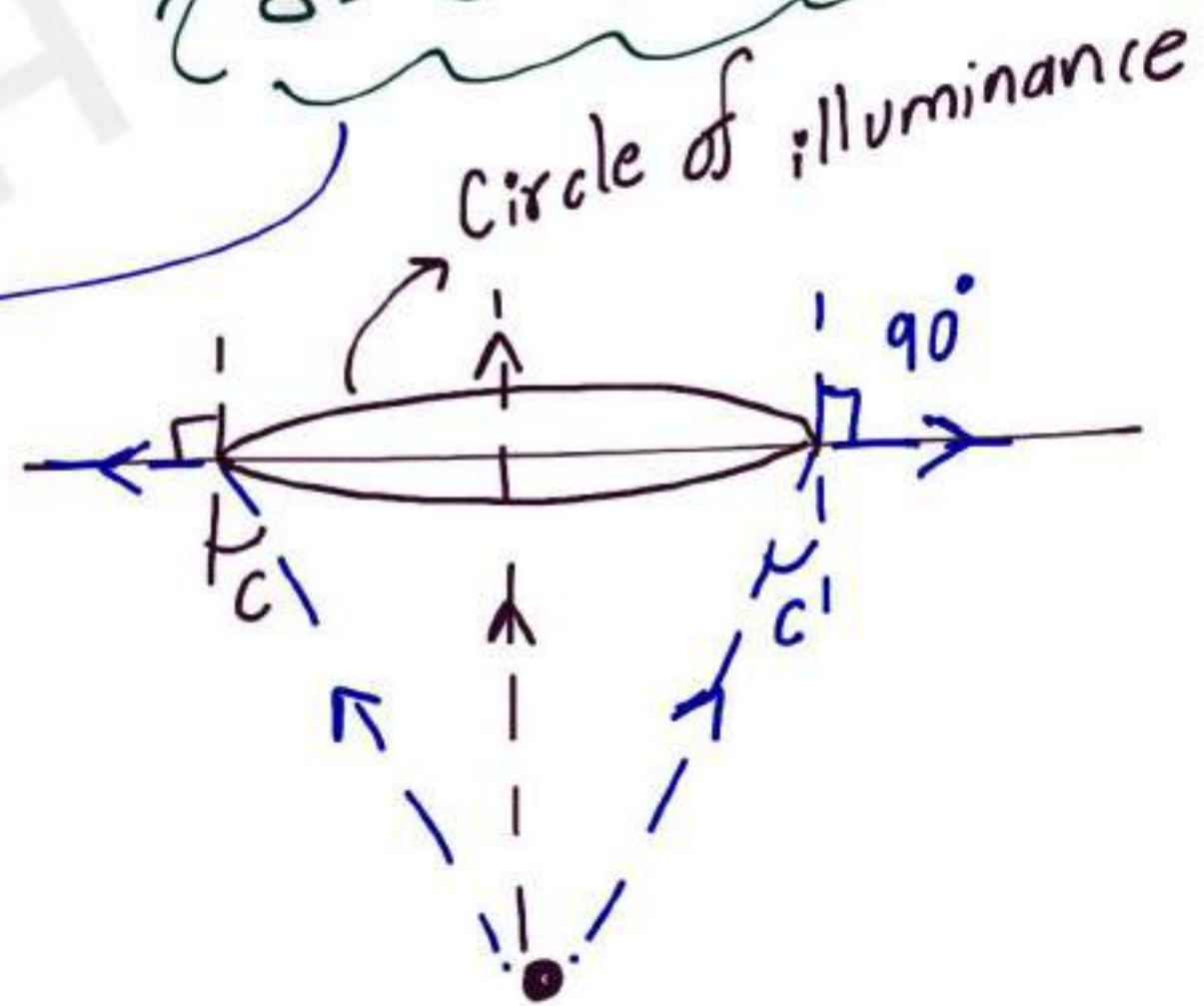
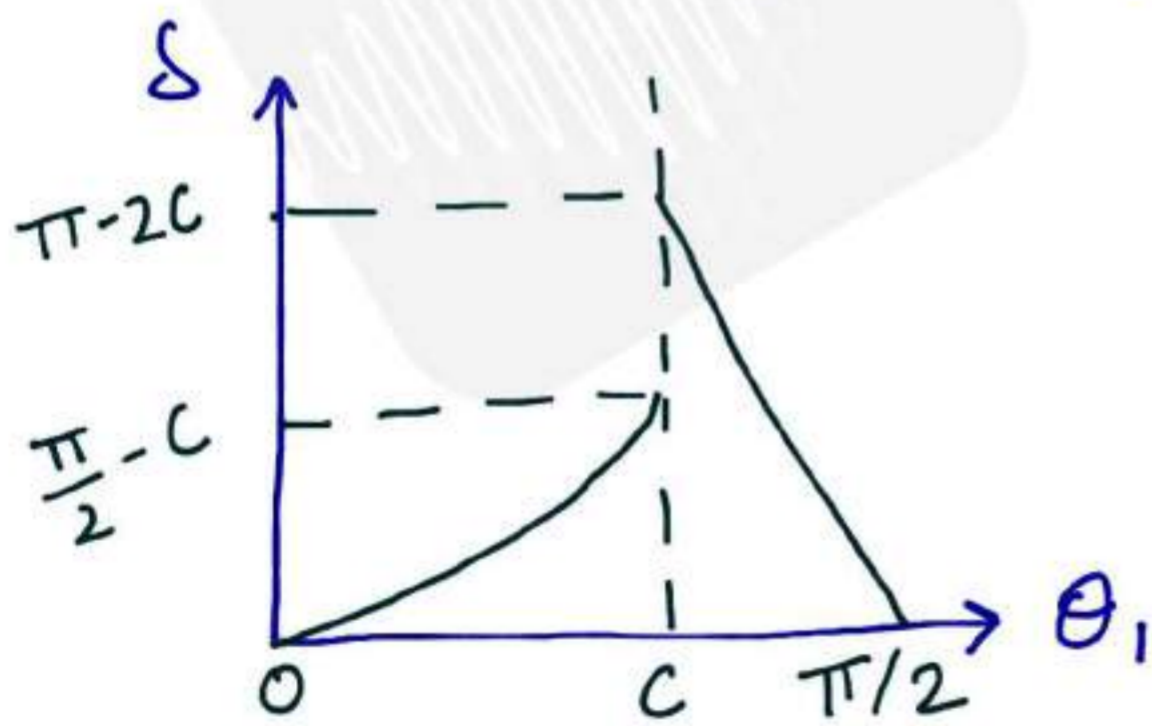


$$\delta_{\max} = \frac{\pi}{2} - c \quad \text{for } \theta_1 \leq c$$

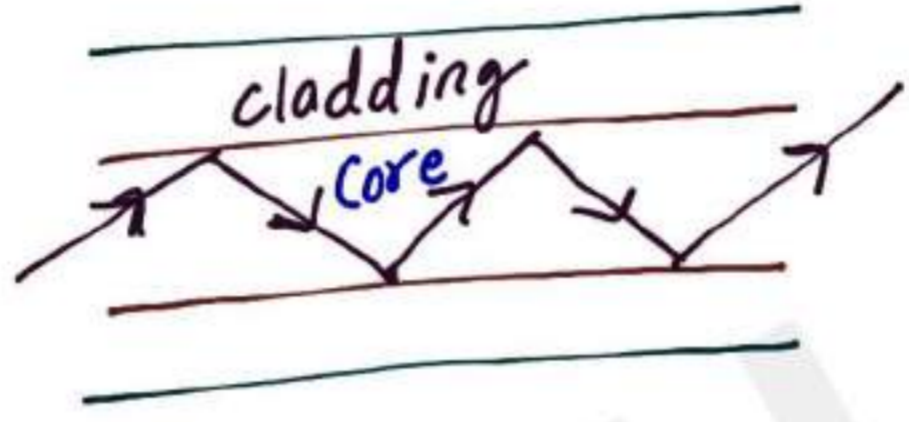
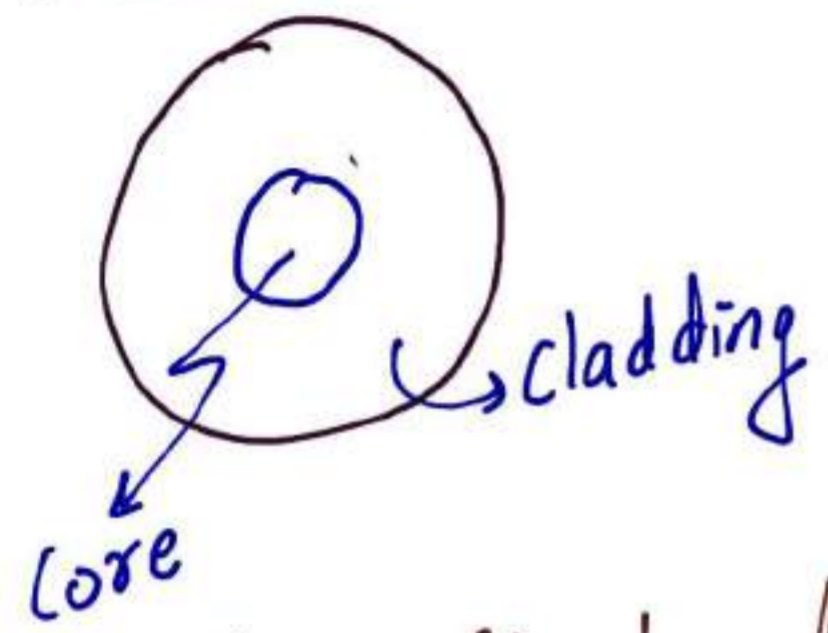
for $\theta_1 > c$

$$\delta = \theta - 2\theta_1$$

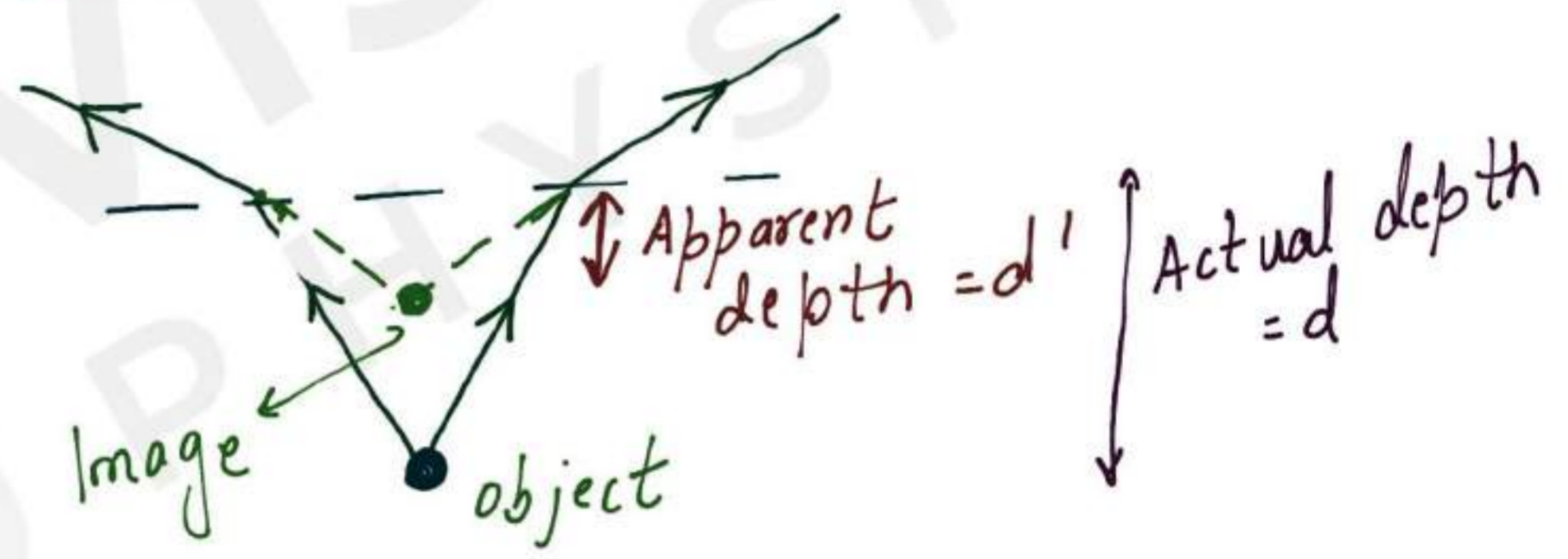
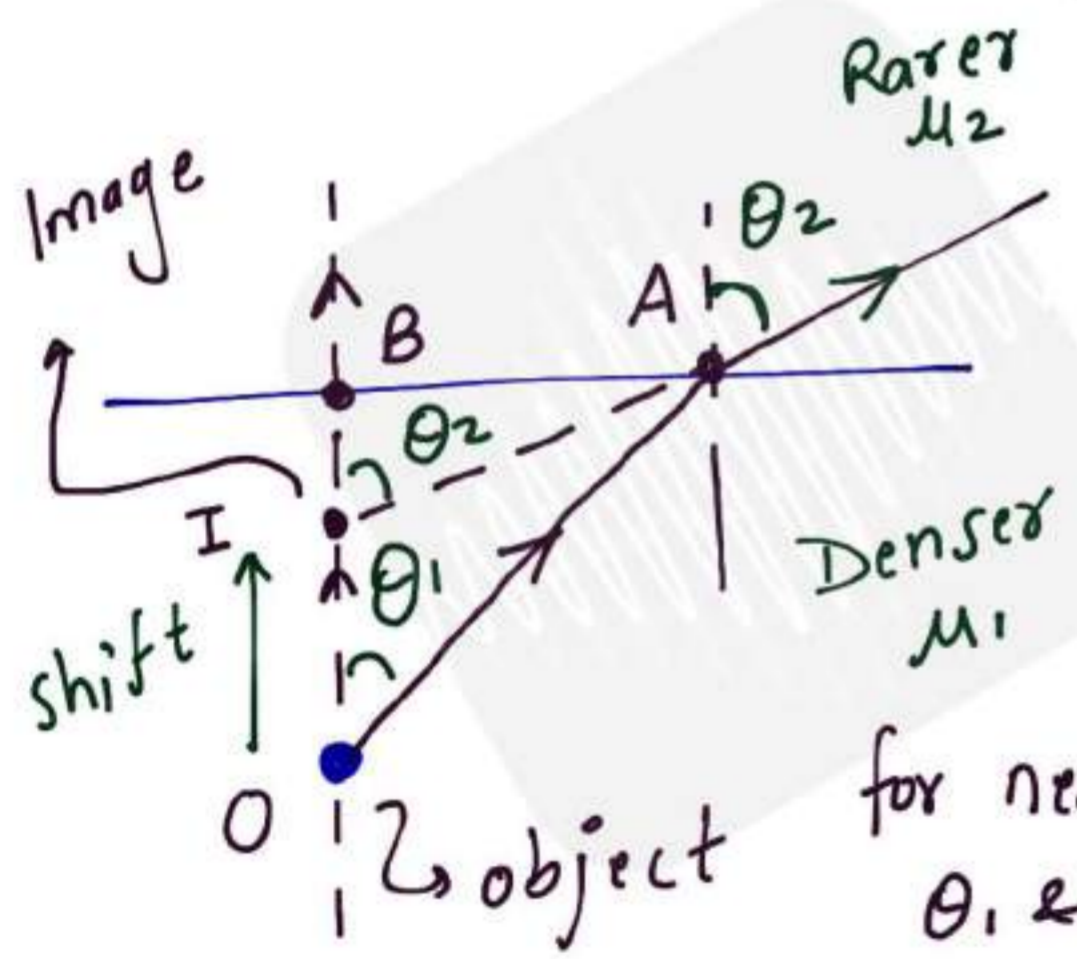
$$\delta_{\max} = \pi - 2c$$



Optical fibres: TIR used for long range information travel



Apparent shift due to refraction:



for nearly normal incident θ_1 & θ_2 will be very small

$$\tan \theta_1 \approx \sin \theta_1 = \frac{AB}{\text{object distance from refracting surface}}$$

$$\tan \theta_2 \approx \sin \theta_2 = \frac{AB}{\text{image distance from refracting surface}}$$

$$\Rightarrow \frac{\sin \theta_1}{\sin \theta_2} = \frac{\tan \theta_1}{\tan \theta_2} = \frac{\text{Image distance from refracting surface}}{\text{object distance from refracting surface}}$$

$$\mu_1 \sin \theta_1 = \mu_2 \sin \theta_2 \Rightarrow \frac{\sin \theta_1}{\sin \theta_2} = \frac{\mu_2}{\mu_1} = \frac{\tan \theta_1}{\tan \theta_2}$$

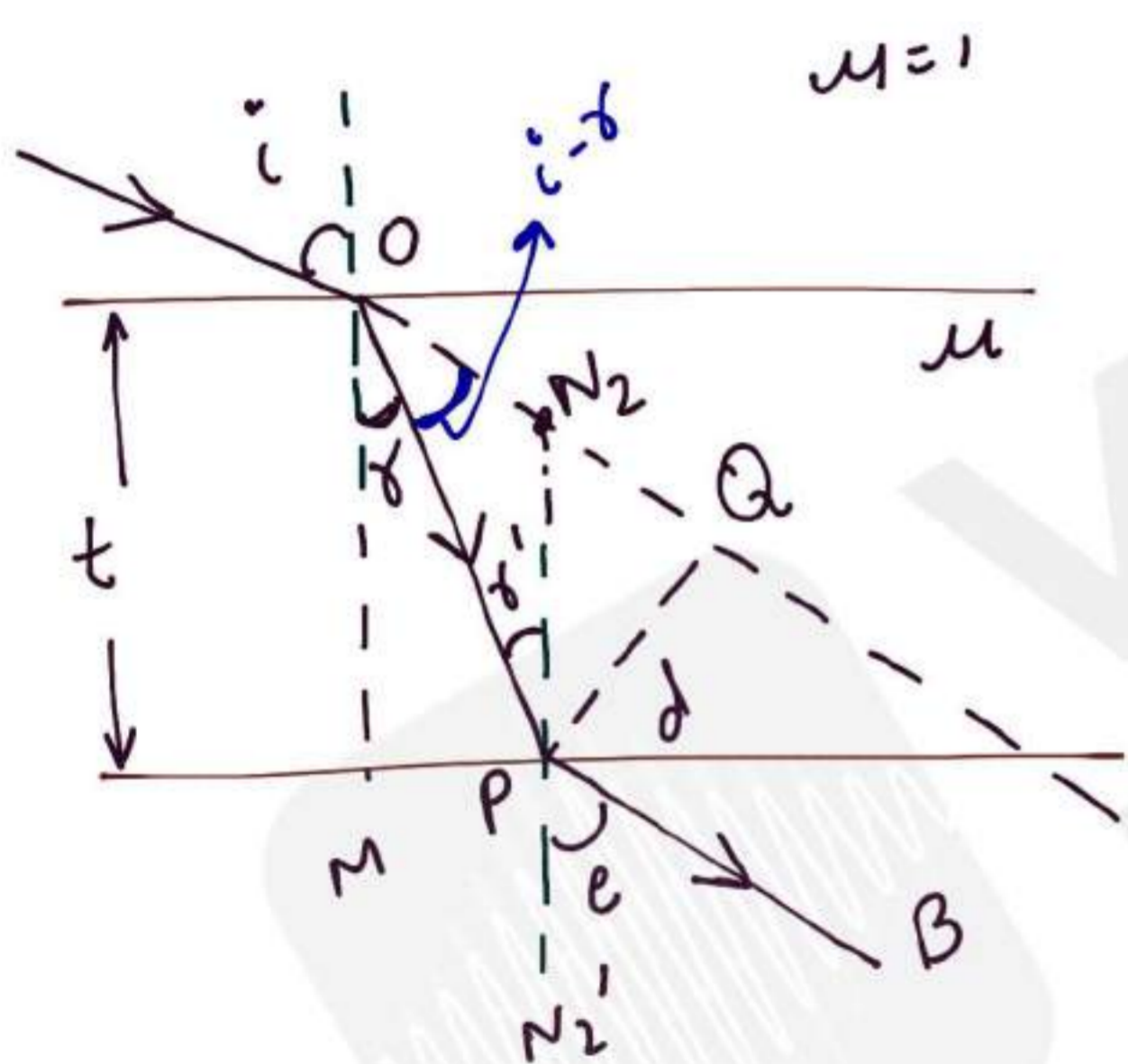
$$\frac{\frac{AB}{OB}}{\frac{OA}{BI}} = \frac{\mu_2}{\mu_1} \Rightarrow \frac{BI}{OB} = \frac{\text{Apparent depth}}{\text{Real depth}} = \frac{\mu_2}{\mu_1}$$

$$\text{Apparent depth} = \frac{\text{Real depth}}{\mu_1 / \mu_2} = \frac{\text{Real depth}}{\mu_{rel}}$$

$$\mu_{rel} = \frac{\mu_i \text{ (RI of medium of incidence)}}{\mu_r \text{ (RI of medium of refraction)}}$$

$$\text{shift} = s = \text{Real depth} - \text{Apparent depth} = \left\{ \text{Real depth} \left(1 - \frac{1}{\mu_{rel}} \right) \right\}$$

Lateral displacement of emergent beam through Glass slab:



if e is angle of emergence from Snell's law:

$$\mu_a \sin i = \mu \sin r \quad \&$$

$$\mu \sin e = \mu_a \sin e'$$

$$e' = r \quad \& \quad \mu_a = 1$$

$$\sin i = \sin e \quad \text{or} \quad (e = i)$$

$$d = PQ = OP \sin(i - r) = \frac{OM \sin(i - r)}{\cos r}$$

$$\left\{ d = \frac{t \sin(i - r)}{\cos r} \right\}$$

for i is very small, r is very small

$$\sin i \rightarrow i, \quad \sin r \rightarrow r \quad \& \quad \cos r \rightarrow 1$$

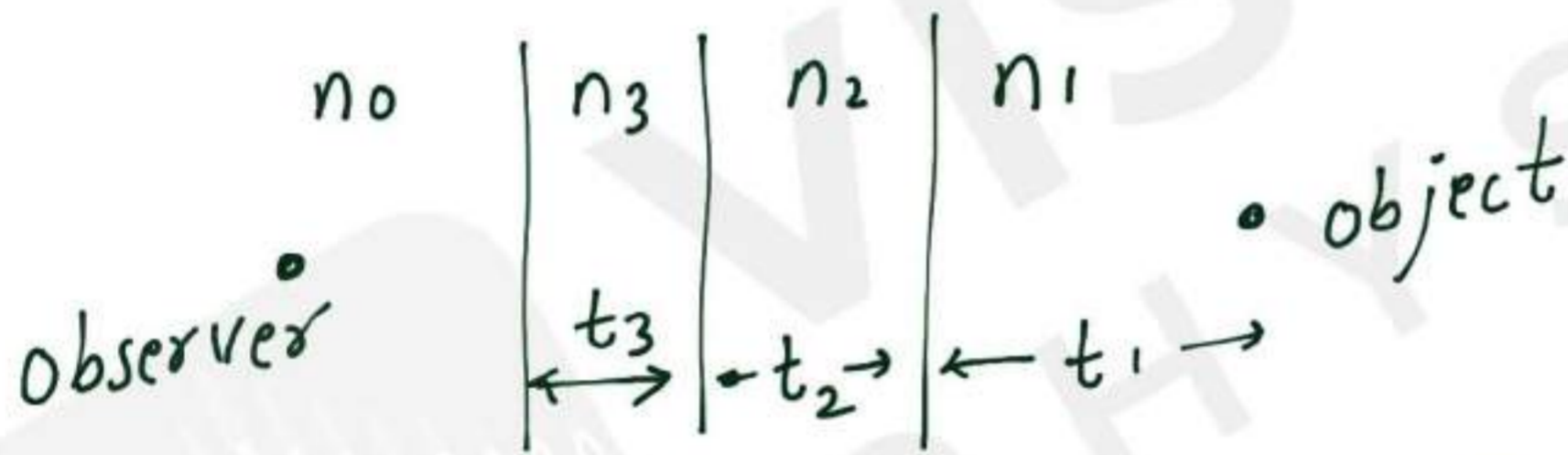
$$\frac{\sin i}{\sin r} = \mu$$

takes the form $\frac{i}{r} = \mu$

$$\Rightarrow d = \frac{t(i-r)}{i} = t i \left(1 - \frac{r}{i}\right)$$

$$\left\{ d = t i \left(1 - \frac{1}{\mu}\right) \right\}$$

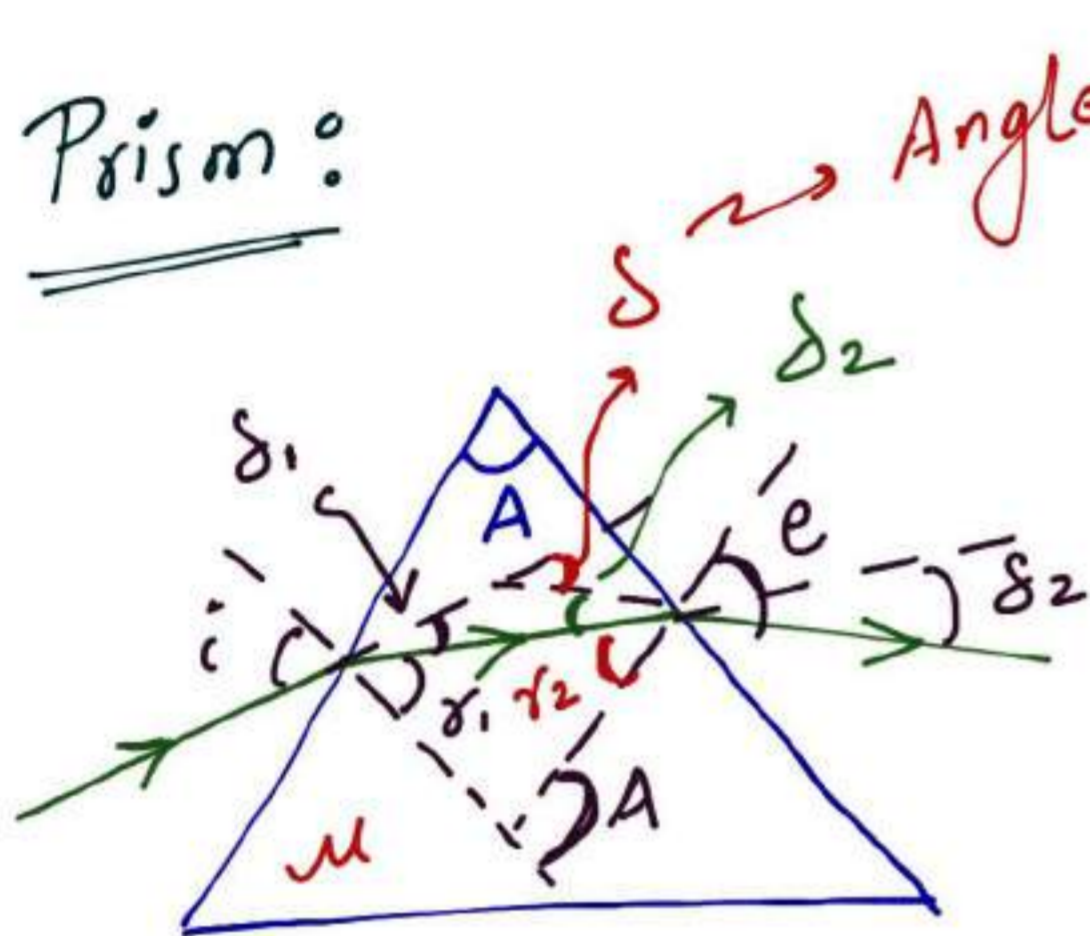
for multiple slabs:



$$\Rightarrow \text{Apparent shift} = t_1 \left[1 - \frac{1}{n_{1 \text{ rel}}}\right] + t_2 \left[1 - \frac{1}{n_{2 \text{ rel}}}\right] + \dots + t_n \left[1 - \frac{1}{n_{n \text{ rel}}}\right]$$

$n_{1 \text{ rel}} = n_1/n_0$, $n_{2 \text{ rel}} = n_2/n_0$ etc.

Prism:



Angle of deviation

↳ Angle between emergent & incident ray

$$\delta_1 = i - r_1, \quad \delta_2 = e - r_2$$

$$\delta = \delta_1 + \delta_2$$

$$\delta = (i - r_1) + (e - r_2)$$

$$\delta = i + e - (r_1 + r_2) \rightarrow A$$

Angle of prism

$$\delta = i + e - A$$

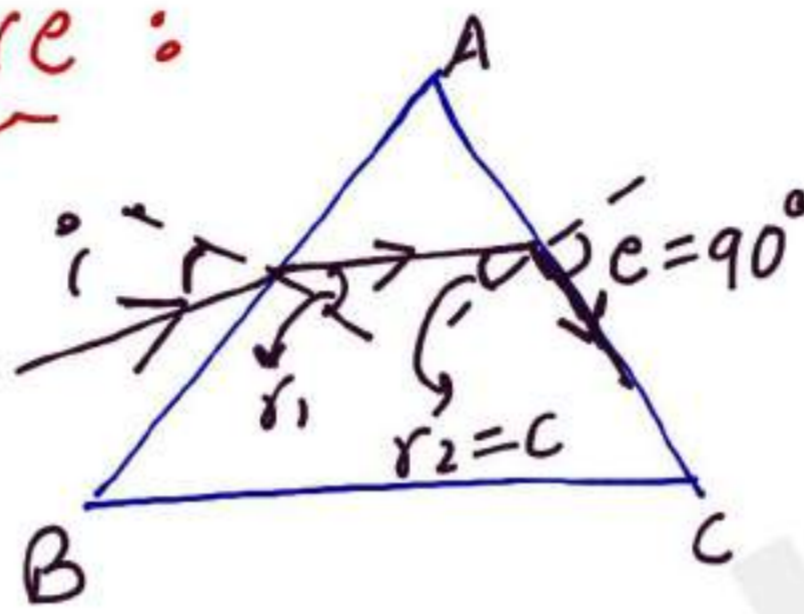
{ if $A > 2\theta_c$ }

↳ critical angle

↳ the ray will not emerge out of a prism (whatever may be the angle of incidence)

$$\mu > \frac{1}{\sin(A/2)}$$

for Grazing emergence:
 $e = 90^\circ$



$$A = \delta_1 + \delta_2 = \delta_1 + C$$

$$\sin C = \frac{1}{n}$$

$$\Rightarrow \sin i = n \sin(A - C)$$

$$= n [\sin A \cos C - \cos A \sin C]$$

$$= n \left[\sin A \sqrt{1 - \sin^2 C} - \cos A \sin C \right]$$

$$= n \left[\sin A \sqrt{1 - \frac{1}{n^2}} - \cos A \times \frac{1}{n} \right]$$

$$\Rightarrow \sin i = n \left[\frac{\sin A}{n} \sqrt{n^2 - 1} - \frac{\cos A}{n} \right]$$

$$\Rightarrow \sin i = \sin A \sqrt{n^2 - 1} - \cos A$$

$$\left\{ i = \sin^{-1} \left[\sqrt{n^2 - 1} \sin A - \cos A \right] \right\}$$

for max Deviation

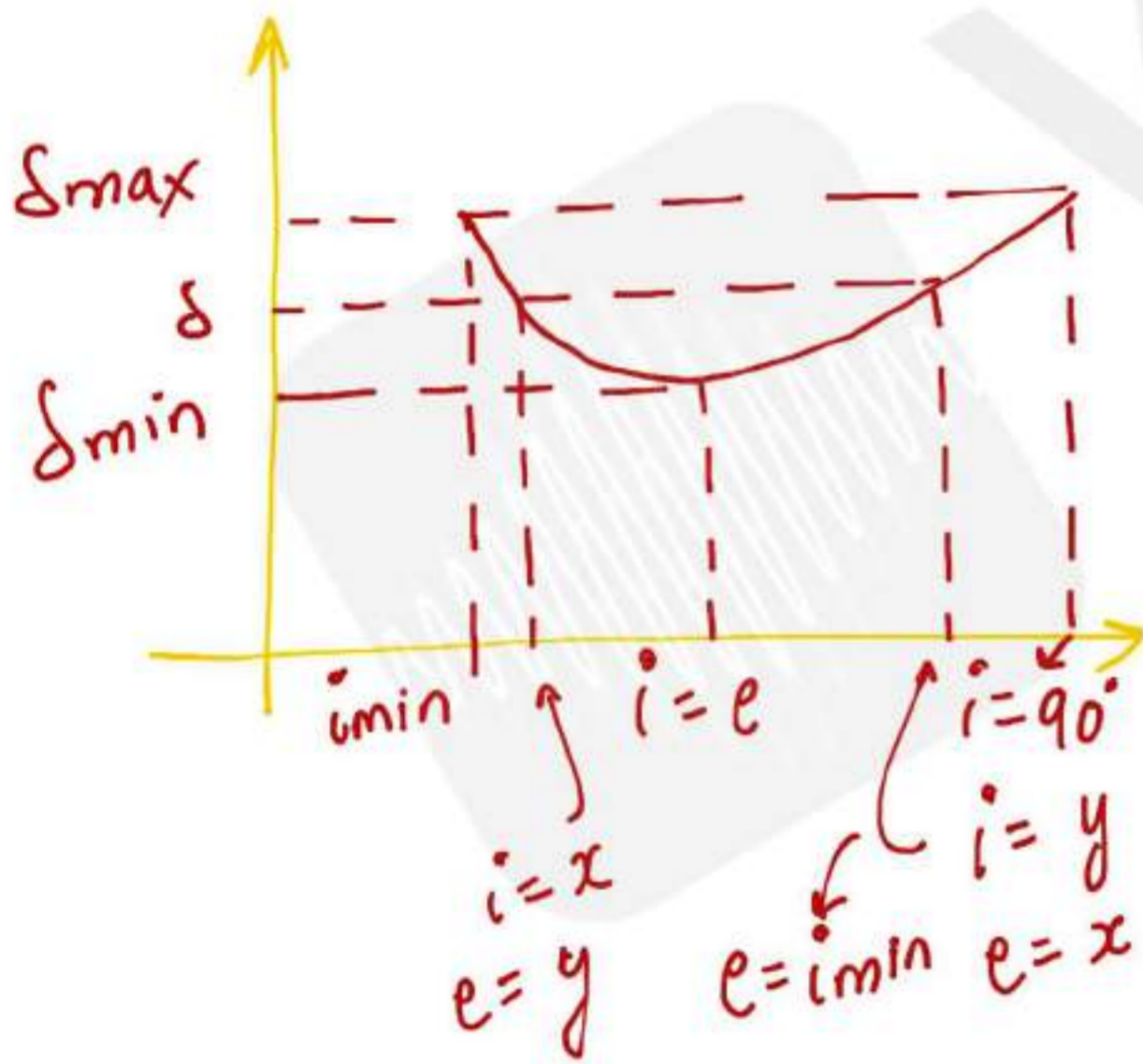
$$\delta_{\max} = 90^\circ + e - A$$

$$e = \sin^{-1} [\mu \sin(A - \theta_c)]$$

for minimum Deviation

$$i^\circ = e, \delta_{\min} = 2i - A$$

$$\mu = \frac{\sin[(\delta_{\min} + A)/2]}{\sin(A/2)}$$



Thin prism

$\hookrightarrow A \rightarrow$ very small
as $A = r_1 + r_2$

\hookrightarrow small as well.
so as i_1 & i_2

$$\sin i_1 = \mu \sin r_1$$

$$i_1 = \mu r_1 \quad [\text{as } i_1, i_2, r_1 \text{ \& } r_2 \text{ are small}]$$

$$\& \sin i_2 = \mu \sin r_2$$

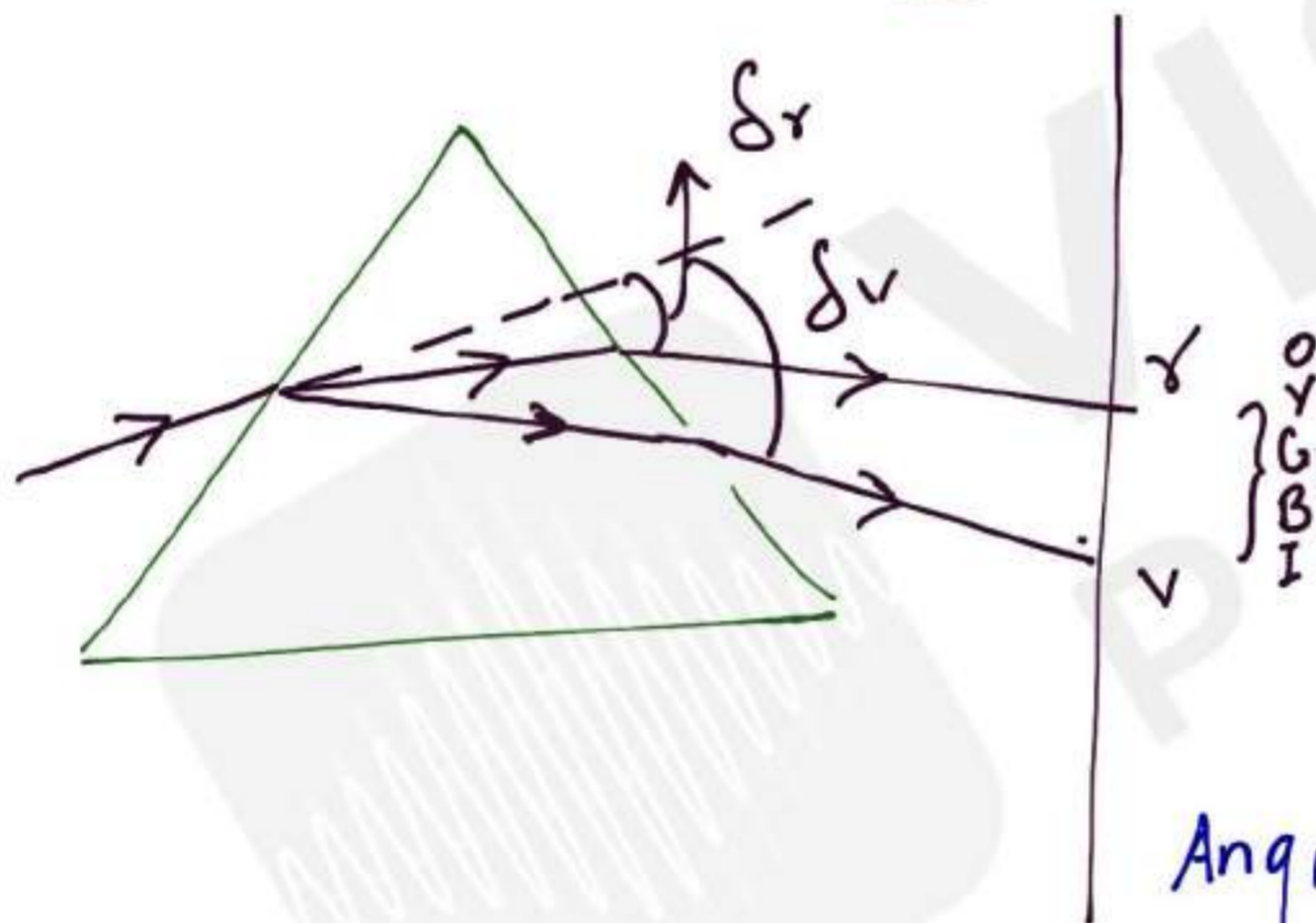
$$i_2 = \mu r_2$$

$$\delta = (i_1 - r_1) + (i_2 - r_2)$$

$$\delta = (\alpha_1 + \alpha_2)(\mu - 1) \Rightarrow \delta = A(\mu - 1)$$

Dispersion of light

when ray of light passes through prism it splits up into rays of constituent colours or wavelength

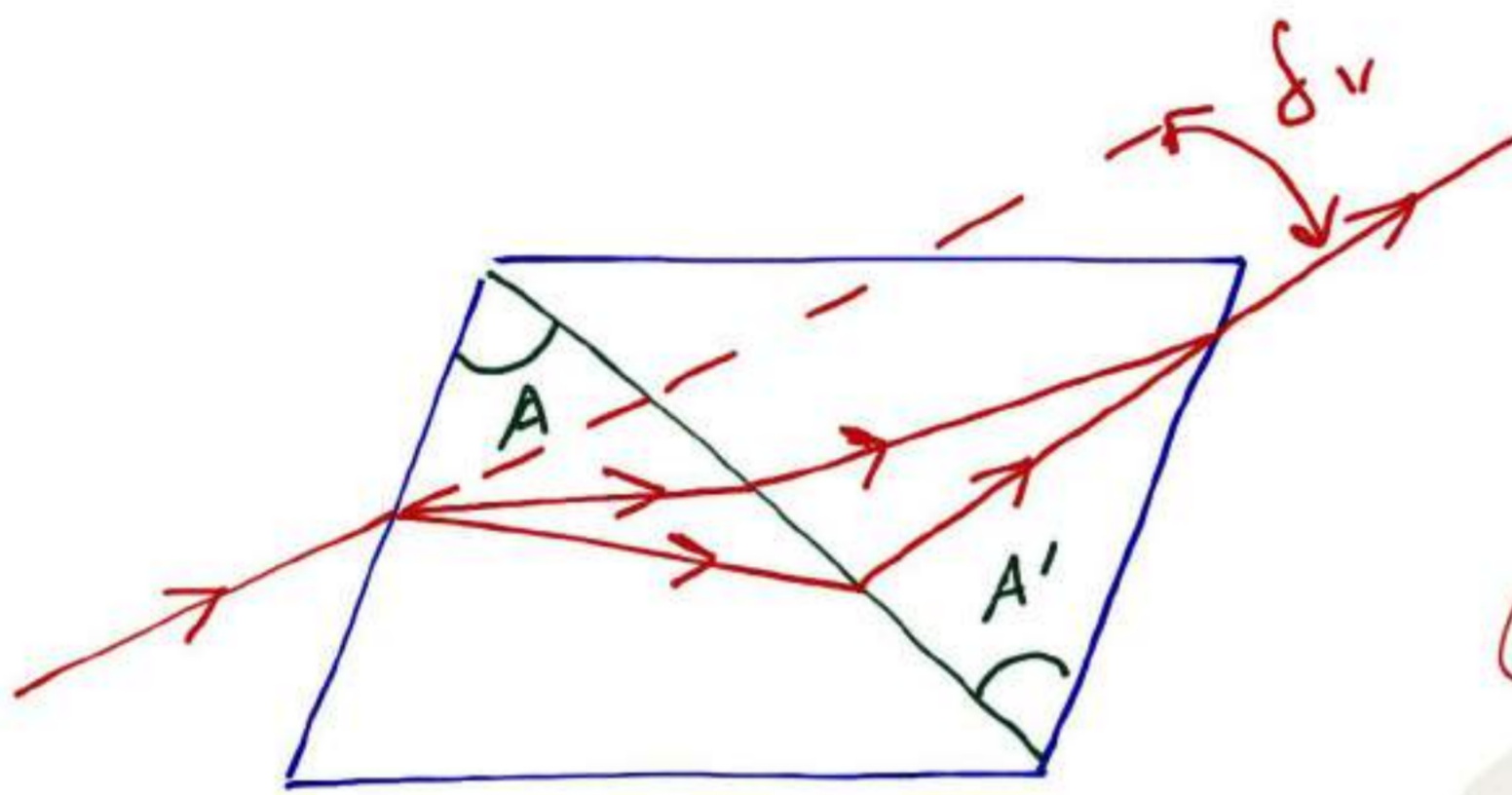


this happens because refractive index varies with wavelength

$$\Rightarrow \mu_{\text{blue}} > \mu_{\text{red}}$$

Angular dispersion: $\theta = \delta_v - \delta_r$

Dispersive power: $\omega = \frac{\delta_v - \delta_r}{\delta}$



for two prism:

$$(\mu_v - \mu_r)A + (\mu_v - \mu_r)A' = 0$$

$$\left\{ A' = \frac{(\mu_v - \mu_r)A}{\mu_v - \mu_r} \right\}$$

$$\omega\delta + \omega'\delta' = 0$$

$$\left\{ \delta = \delta' \left[1 - \frac{\omega}{\omega'} \right] \right\}$$

ω & ω' → dispersive powers of two prism

δ & δ' → mean deviations